

## MATHEMATICS ( Subjective ) Group – I

Time: 02:30 Hours Marks: 80

FSD-1-24

## SECTION – I

## 2. Attempt any EIGHT parts:

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- (i) State Golden rule of fractions and rule for quotient of fractions.
- (ii) Find multiplicative inverse of  $(\sqrt{2}, -\sqrt{5})$
- (iii) Prove that sum as well as product of two conjugate complex numbers is a real.
- (iv) Simplify:  $(a + bi)^{-2}$
- (v) Write power set of  $A = \{9, 11\}$
- (vi) If  $a, b$  are elements of a group  $G$ , then show  $(ab)^{-1} = b^{-1}a^{-1}$
- (vii) If  $A = \begin{bmatrix} i & 1+i \\ 1 & -i \end{bmatrix}$ , show that  $A - (\bar{A})^t$  is skew-Hermitian.
- (viii) Evaluate:  $\begin{vmatrix} 1 & 2 & -3 \\ -1 & 3 & 4 \\ -2 & 5 & 6 \end{vmatrix}$
- (ix) If  $A = \begin{bmatrix} 2i & i \\ i & -i \end{bmatrix}$  then find  $A^{-1}$
- (x) Find  $k$  if  $x^3 + kx^2 - 7x + 6$  has remainder  $-4$ , when divided by  $x + 2$ .
- (xi)  $\alpha, \beta$  are roots of  $5x^2 - x + 2 = 0$ , find  $\frac{3}{\alpha} + \frac{3}{\beta}$
- (xii) Discuss the nature of roots of  $x^2 - 5x + 6 = 0$

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## 3. Attempt any EIGHT parts:

- (i) Define rational fraction.
- (ii) Resolve into partial fractions  $\frac{x^2 + x - 1}{(x + 2)^3}$
- (iii) Define sequence.
- (iv) If the 5th term of an AP is 13 and its 17th term is 49, find its general term.
- (v) Find vulgar fraction equivalent to  $1.\dot{5}\dot{3}$  recurring decimal.
- (vi) Find the 12th term of harmonic sequence  $\frac{1}{3}, \frac{2}{9}, \frac{1}{6}, \dots$
- (vii) Evaluate:  $\frac{10!}{7!}$
- (viii) Define sample space.
- (ix) Find the value of  $n$  if  ${}^nC_{10} = \frac{12 \times 11}{2!}$
- (x) Show that  $5^n - 1$  is divisible by 4 if  $n = 5$ .
- (xi) Expand  $(1 - 2x)^{\frac{1}{3}}$  up to 4 terms.
- (xii) Find the middle term of  $\left(\frac{x}{2} + \frac{2}{x^2}\right)^{12}$

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## 4. Attempt any NINE parts:

- (i) If  $\cos \theta = -\frac{\sqrt{3}}{2}$  and the terminal arm of the angle is in III quadrant, find the value of  $\sin \theta$  and  $\tan \theta$
- (ii) Verify that  $\cos 2\theta = 2\cos^2 \theta - 1$  when  $\theta = 30^\circ$
- (iii) Show that  $\cos(\alpha + \beta)\cos(\alpha - \beta) = \cos^2 \beta - \sin^2 \alpha$
- (iv) Prove that  $\cot \alpha - \tan \alpha = 2\cot 2\alpha$
- (v) Prove that  $\frac{\sin 3x - \sin x}{\cos x - \cos 3x} = \cot 2x$
- (vi) What is the domain and range of  $y = \cos x$ ?

(Continued P.....2)

- (vii) Find the period of  $3\cos \frac{x}{5}$
- (viii) Draw the graph of  $y = \sin x$  for  $0 \leq x \leq 360^\circ$ .
- (ix) Find the measure of the greatest angle if sides of triangle are 16, 20, 33.
- (x) Find the area of the triangle ABC, when  $b = 37$ ,  $c = 45$ ,  $\alpha = 30^\circ 50'$
- (xi) Prove that  $r_1 r_2 r_3 = rs^2$
- (xii) Prove that  $2\tan^{-1} A = \tan^{-1} \frac{2A}{1-A^2}$
- (xiii) Find the solution of equation  $\sec x = -2$ ,  $x \in [0, 2\pi]$

**SECTION - II** Attempt any THREE questions. Each question carries 10 marks.

5. (a) If  $A = \begin{bmatrix} 1 & -1 \\ a & b \end{bmatrix}$ ,  $A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ , find the values of  $a$  and  $b$ .

- (b) Solve the system of equations  $x^2 - 5xy + 6y^2 = 0$ ;  $x^2 + y^2 = 45$

6. (a) Resolve into partial fractions:  $\frac{x^4}{1-x^4}$

- (b) If  $y = 1 + 2x + 4x^2 + 8x^3 + \dots$  show that  $x = \frac{y-1}{2y}$

7. (a) Prove that  ${}^nC_r + {}^nC_{r-1} = {}^{n+1}C_r$

- (b) If  $2y = \frac{1}{2^2} + \frac{1 \cdot 3}{2!} \cdot \frac{1}{2^4} + \frac{1 \cdot 3 \cdot 5}{3!} \cdot \frac{1}{2^6} + \dots$ , then prove that  $4y^2 + 4y - 1 = 0$

8. (a) Find  $\sin(\alpha + \beta)$  and  $\cos(\alpha + \beta)$ , given that  $\tan \alpha = -\frac{15}{8}$  and  $\sin \beta = -\frac{7}{25}$  and neither the terminal side of the angle of measure  $\alpha$  nor that of  $\beta$  is in the IV quadrant.

- (b) Prove that  $r_1 r_2 + r_2 r_3 + r_3 r_1 = s^2$

9. (a) Prove the identity, state the domain of  $\theta$ ,  $\sin^6 \theta + \cos^6 \theta = 1 - 3\sin^2 \theta \cos^2 \theta$

- (b) Prove that  $\tan^{-1} \frac{120}{119} = 2 \cos^{-1} \frac{12}{13}$

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