# A-PDF Watermark DEMO:

## FEDERAL PUBLIC SERVICE COMMISSION MO: Purchase Composition Purchase Composition FOR RECRUITMENT TO POSTS IN BS-17 UNDER THE FEDERAL GOVERNMENT

### **PURE MATHEMATICS**

TIME ALLOWED: THREE HOURS MAXIMUM MA			
NOTI		Attempt FIVE questions in all by selecting TWO Questions each from SECTION-A& ONE Question from SECTION-C. ALL questions carry EQUAL marks. All the parts (if any) of each Question must be attempted at one place instead of at discussion.	
		<ul> <li>places.</li> <li>Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.</li> <li>No Page/Space be left blank between the answers. All the blank pages of Answer Book mube crossed.</li> </ul>	
	(v) (vi)	Extra attempt of any question or any part of the attempted question will not be considered <b>Use of Calculator is allowed.</b>	1.
SECTION-A			
Q. 1.	<b>(a)</b>	Prove that the normaliser of a subset of a group $G$ is a Subgroup of $G$ . (10)	))
	(b)	Let $A$ be a normal subgroup and $B$ a subgroup of a group $G$ . Then prove that $\langle A,B \rangle = AB$ (10)	)) <b>(20)</b>
Q. 2.	(a)	Let <i>a</i> be a fixed point of a group <i>G</i> and consider the mapping $I_a$ : $G \rightarrow G$ defined (10 by $I_a(g) = aga^{-1}$ where $g \in G$ .	)
		Show that $I_a$ is an automorphism of $O$ . The show that for $u_i$ $O = O$ , $I_a : I_b = I_{ab}$	)) (20)
	(b)	Let $M_2(R) = \left\{ \begin{bmatrix} a & b \\ c & d \end{bmatrix} : a, b, c, d \in R \right\}$ be the set of all 2×2 matrices with	
		real entries. Show that ( $M_2(R)$ , +, · ) forms a ring with identity. Is ( $M_2(R)$ , +, · ) a field?	
Q. 3.	<b>(a)</b>	Let $T: X \rightarrow Y$ be a linear transformation from a vector space X into a Vector (10) space Y. Prove that Kernal of T is a subspace.	))
	(b)	Find the value of $\lambda$ such that the system of equations (10)	)) (20)
		$x + \lambda y + 3z = 0$	
		$4x + 3y + \lambda z = 0$	
		2x + y + 2z = 0	
		has non-trivial solution.	
		<u>SECTION-B</u>	
Q. 4.	(a)	Using $\delta - \epsilon$ definition of continuity, prove that the function $Sin^2 x$ is continuous (10) for all $x \in \mathbb{R}$ .	
	(b)	Find the asymptotes of the curve $(x^2 - y^2)(x + 2y) + 5(x^2 + y^2) + x + y = 0$ (10)	(20)
Q. 5.	(a)	Prove that the maximum value of $\left(\frac{1}{x}\right)^x$ is $e^{1/e}$ (10)	

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- **Q. 6.** (a) Find the area enclosed between the curves  $y=x^3$  and y=x. (10)
  - (b) A plane passes through a fixed point (a, b, c) and cuts the coordinate axes in (10) (20) A,B,C. Find the locus of the centre of the sphere OABC for different positions of the plane, O is the origin.

#### **SECTION-C**

Q. 7. (a) Determine <sup>P(z)</sup> where (10)
P(z)=(z-z<sub>1</sub>)(z-z<sub>2</sub>)(z-z<sub>3</sub>)(z-z<sub>4</sub>) with z<sub>1</sub> = e<sup>iπ/4</sup>, z<sub>2</sub> = z
<sub>1</sub>, z<sub>3</sub> = -z<sub>1</sub> and z<sub>4</sub> = -z
<sub>1</sub>.
(b) Find value of the integral ∫<sub>c</sub>(z - z
<sub>0</sub>)<sup>n</sup> d z, (n any integer) along the circle C (10) (20) .....with centre and z
<sub>0</sub> radius r, described in the counter clock wise direction.
Q. 8. (a) Use Cauchy Integral Formula to evaluate ∫<sub>c</sub> c o h z + s i 2 z / z - T/2 dz along the simple closed counter C: | z |=3 described in the positive direction.
(b) State and prove Cauchy Residue Theorem. (10) (20)

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