

## FEDERAL PUBLIC SERVICE COMMISSION D: Purchase fcommantave Baranna for Recruitment to Posts in BS-17 UNDER THE FEDERAL GOVERNMENT



## **APPLIED MATHEMATICS**

TIME ALLOWED: THREE HOURS			MAXIMUM MARKS = 100		
<ul> <li>NOTE:(i) Attempt ONLY FIVE questions. ALL questions carry EQUAL marks</li> <li>(ii) All the parts (if any) of each Question must be attempted at one place instead of at different places.</li> <li>(iii) Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper.</li> <li>(iv) No Page/Space he left blank between the answers. All the blank pages of Answer Book must</li> </ul>					
<ul> <li>(v) No rage space be left blank between the answers. An the blank pages of Answer book must be crossed.</li> <li>(vi) Extra attempt of any question or any part of the attempted question will not be considered.</li> <li>(v) Use of Calculator is allowed.</li> </ul>					
Q. No. 1.	(a)	Prove that $\nabla \cdot \left[\frac{f(r)\vec{r}}{r}\right] = \frac{2}{r}f(r)$	) + f'(r)	(10)	
	(b)	Verify Stokes' theorem for $\vec{A}$ = the upper half surface of the spl boundary.	$(2x - y)\hat{i} - yz^{2}\hat{j} - y^{2}z\hat{k}$ , where S is here $x^{2} + y^{2} + z^{2} = 1$ and C is its	(10)	
Q. No. 2.	(a)	Forces P, Q, R act at a point paralle same order. Show that the magnitu	el to the sides of a triangle ABC taken in the de of the resultant force is	(10)	
		$\sqrt{\mathbf{P}^2 + \mathbf{Q}^2 + \mathbf{R}^2 - 2\mathbf{Q}\mathbf{R}}$	$\cos A - 2 R P \cos B - 2 P Q \cos C$		
	(b)	Find the distance from the cusp of the	he centroid of the region bounded by the	(10)	
		cardioid $r = a (1 + \cos \theta)$ .			
Q. No. 3.	(a)	A particle describes simple harm acceleration at a point P are u an at another point Q are v and g. I	onic motion in such a way that its velocity and ad f respectively and the corresponding quantities Find the distance PQ.	(10)	
	(b)	Derive the radial and transverse co	mponents of velocity and acceleration of a particle.	(10)	
Q. No. 4.	Solve	Solve the following differential equations:			
	(a)	$\frac{dy}{dx} + \frac{y}{x} = x^3 y^4$		(10)	
	(b)	$(D^2 - 5D + 6) y = x^3 e^{2x}$		(10)	
Q. No. 5.	<b>(a)</b>	Solve the differential equation us $\frac{d^2 y}{d x^2} + y = \tan x$ , $-\frac{\pi}{2} < $	sing the method of variation of parameters $x < \frac{\pi}{2}$	(10)	
	(b)	Solve the Euler – Cauchy differe	ntial equation $x^2 y'' - 3 x y' + 4y = x^2 \ln x$ .	(10)	
Q. No. 6.	(a) F	ind the Fourier series of the follow $\int -x  \text{if } -\pi < x < 0$	ring function: 0	(10)	
	(b) S	$x$ if $0 < x < \pi$ olve the initial - boundary value pr	roblem:	(10)	

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- Q. No. 7. (a) Apply Newton Raphson method to find the smaller positive root of the equation (10)  $x^2 - 4x + 2 = 0$ 
  - (b) Solve the following system of equations by Gauss Seidel iterative method by (10) taking the initial approximation as  $x_1 = 0$ ,  $x_2 = 0$ ,  $x_3 = 0$ :

$$5x_1 + x_2 - x_3 = 4$$
  

$$x_1 + 4x_2 + 2x_3 = 15$$
  

$$x_1 - 2x_2 + 5x_3 = 12$$

Q. No. 8.

(a) Approximate  $\int_{0}^{1} \frac{dx}{1+x^2}$  using

(i) Trapezoidal rule with n = 4 (ii) Simpson's rule with n = 4 Also compare the results with the exact value of the integral.

(b) Apply the improved Euler method to solve the initial – value problem: y' = x + y, y(0) = 0

by choosing h = 0.2 and computing  $y_1, \dots, y_5$ .

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(10)

(10)