

Mathematics Part-II

Fic. No. _____

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Mathematics Part-II

Time: 20 Min

SECTION "A"

Marks: 20

NOTE: Use this sheet for this section. No marks will be awarded for cutting, erasing or overwriting.**Q1. Choose the correct answer from the given choices i.e. (a, b, c, d) and insert into the relevant box.**

- (i). $\lim_{x \rightarrow 4} (\log_4 x) (\log_4 x^2)$ (A) 2 (B) 16 (C) 10 (D) 9
- (ii). If $x = t^4$ $y = t^3$ then $\frac{dy}{dx} =$ _____ (A) $\frac{3}{4}$ (B) $\frac{3}{4t}$ (C) $\frac{1}{t}$ (D) t
- (iii). $\frac{d}{dx} (\tan \alpha \tan \alpha S) =$ _____ (A) 0 (B) $\cos \alpha \sec^2 \alpha$ (C) $\tan \alpha \cos x$ (D) None
- (iv). $\int e^{\cos x} \sin x \, dx =$ _____ (A) $-e^{\cos x}$ (B) $\sin x$ (C) $-e^{\sin x}$ (D) None
- (v). $\int_2^3 f(x) + \int_3^2 f(x) \, dx =$ _____ (A) 0 (B) $\int_2^3 f(x)$ (C) $\int_2^3 f(x) \, dx$ (D) None
- (vi). The Angle between two straight lines L_1, L_2 then $\tan \phi =$ _____.
 (A) $\frac{m_2 - m_1}{1 + m_1 m_2}$ (B) $\frac{m_1 + m_2}{1 - m_1 m_2}$ (C) $\frac{m_2 + m_1}{1 - m_1 m_2}$ (D) NONE
- (vii). The Length of the Latus-Rectum to ellipse $16x^2 + 25y^2 = 400$.
 (A) 8 (B) 10 (C) $\frac{32}{5}$ (D) 8
- (viii). The line $y = mx + c$ passes through origin then .
 (A) $y = mx$ (B) $y = mx + c$ (C) $y = 0$ (D) 0
- (ix). The Perpendicular distance from origin then .
 (A) $d = c$ (B) $d = \frac{ax + by}{\sqrt{a^2 + b^2}}$ (C) $\frac{c}{\sqrt{a^2 + b^2}}$ (D) 0
- (x). The angle of inclination for the line parallel to $y - x$ is $\phi \neq$
 (A) 90° (B) 75° (C) 45° (D) 60°
- (xi). The line $y = mx + c$ Tangent to ellipse. If $c^2 =$
 (A) $c^2 = a^2 m^2 - b^2$ (B) $c^2 = a^2 m^2 + b^2$ (C) $c = \frac{a}{m}$ (D) None
- (xii). The asymptotes of hyperbola.
 (A) $y = \pm \frac{bx}{a}$ (B) $y = \pm \frac{ax}{b}$ (C) $x = \pm \frac{by}{a}$ (D) None
- (xiii). The distance between foci to ellipse $25x^2 + 16y^2 = 400$ is _____
 (A) 6 (B) 10 (C) 7 (D) 8
- (xiv). The equation of direct in to parabola $y^2 = 8x$ is _____
 (A) $x - a = 0$ (B) $x + a = 0$ (C) $x + 2 = 0$ (D) $x - 2 = 0$
- (xv). The volume of Parellopiped are _____
 (A) $|a \cdot b \times c|$ (B) $|a \times b|$ (C) $|a \cdot C \times b|$ (D) $|a \times c|$
- (xvi). If Two vectors a and b are Perpendicular to each other if $a \cdot b =$
 (A) 0 (B) 1 (C) 2 (D) -1
- (xvii). Length of the vector $|a| = |4i + 7j + 2k| =$ _____
 (A) $\sqrt{69}$ (B) 9 (C) 7 (D) 5
- (xviii). $\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{2x} =$ _____ (A) 1 (B) 0 (C) 2 (D) 4
- (xix). $\lim_{x \rightarrow 0} \frac{\sin px}{qx} =$ _____ (A) 1 (B) $\frac{p}{q}$ (C) 0 (D) 2
- (xx). $\int e^{2x} \, dx =$ _____ (A) $\frac{e^{2x+1}}{2x+1}$ (B) e^{2x} (C) $\frac{e^{2x}}{2}$ (D) 0

Mathematics Part-II

Time: Allowed: 2.40h

Marks: 80

SECTION "B"**Marks: 50****Q2. Attempt any Ten (10) questions. All question carry equal Marks.**

- (i) $f(x) = x - 4$ $g(x) = 3x - 2$ Find $f \circ g^{-1}$
- (ii) $\lim_{x \rightarrow 2} \frac{\sqrt{x+7} - 3}{x-2}$
- (iii) $y = x + \sqrt{x}$ Differentiate w-r-t abinito method.
- (iv) $\frac{y}{x} = \tan^{-1} \frac{x}{y}$ Find $\frac{dy}{dx} = \frac{y}{x}$
- (v) Use differential to Find approximate value of $\sqrt[3]{61}$
- (vi) $\int \cos^3 3x dx$
- (vii) $\int \frac{e^{2x}}{1+e^2}$
- (viii) Use distance Formula show that A(3,1) B(6,2) C(9,3) are collinear.
- (ix) Are the pair of lines are Parallel if yes then Find distance between $6x + 8y + 16 = 0$ and $3x + 4y - 12 = 0$
- (x) Find the equation of circle whose centre (3,4) and which contain (8,9).
- (xi) Show that the line $y = mx + \frac{a}{m}$ is tangent to Parabola $y^2 = 4ax$.
- (xii) Find the eccentricity of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$; if its latus-Rectum be equal to half of its minor axis.
- (xiii) Use the usual notation prove that in triangle ABC. $a = b \cos \gamma + c \cos \beta$

SECTION "C"**Marks: 30****Note: Attempt any THREE questions. All questions carry equal marks.**

- Q3. (A) $\lim_{x \rightarrow 0} \frac{e^{\frac{1}{x}} - 1}{e^{\frac{1}{x}} + 1}$ $x < 0$ (B) $y = \sin(\sin x)$ Prove that $y'' + \tan xy + y \cos^2 x$
- Q4. (A) $\int_0^{\frac{3\pi}{4}} |\cos x| dx$ (B) $\int \frac{dx}{25 - 16x^2}$
- Q.5 (A) Find the Points Trisecting the line Segment joining the points A(2,1) B(3,6).
(B) Find angle θ Form line $l_1 = x - sy + 3 = 0$ and $l_2 = 3u - y + 7 = 0$
- Q.6 (A) For what value of a. the circle $x^2 + y^2 - 2ax - 4 = 0$ will Touch the line $x - 2y = 6$
(B) Find the Value of P for which the line $x \cos \alpha + y \sin \alpha = P$ Touch the ellipse