

**Mathematics Part-I**

Fic. No. \_\_\_\_\_

**Mathematics Part-I**  
**SECTION "A"**

Fic. No. \_\_\_\_\_

Time: 20 Min

Marks: 20

**NOTE: Use this sheet for this section. No marks will be awarded for cutting, erasing or overwriting.**

Q1. Choose the correct answer from the given choices i.e. (a, b, c, d) and insert into the relevant box.

- (i).  $(-i)^{-19} =$  \_\_\_\_\_.  
(A)  $i$  (B)  $-i$  (C)  $1$  (D)  $-1$
- (ii). A group G is called abelian group if it has \_\_\_\_\_.  
(A) Distributive prop (B) Associative prop (C) Commutative prop (D) Identity
- (iii). If  $z = a + ib$  then  $|\frac{1}{z}| =$  \_\_\_\_\_.  
(A)  $a^2 - b^2$  (B)  $a^2 + b^2$  (C)  $\sqrt{a^2 + b^2}$  (D)  $\sqrt{a^2 - b^2}$
- (iv). If A is a square Matrix and  $|A| = 0$  the  $A^{-1} =$  \_\_\_\_\_.  
(A)  $A$  (B)  $\frac{1}{|A|} adj A$  (C) Not exist (D)  $-A$
- (v). If A is a square Matrix of order n the cofactor of the element  $a_{ij}$  i.e  $A_{ij} =$  \_\_\_\_\_.  
(A)  $(-1)^{i+j} M_{ij}$  (B)  $M_{ij}$  (C)  $-M_{ij}$  (D)  $(-1)^{i+i} M_{ij}$
- (vi). The equation  $4x^2 + x + 1 = 0$  has \_\_\_\_\_ roots.  
(A) Real (B) Imaginary (C) Complex (D) None
- (vii).  $\omega^{-5} =$  \_\_\_\_\_. Where  $\omega$  is a cube root of unity.  
(A)  $1$  (B)  $0$  (C)  $\omega$  (D)  $\omega^2$
- (viii). If the roots of the quadratic equation are rational then \_\_\_\_\_.  
(A)  $b^2 - 4ac = 0$  (B)  $b^2 - 4ac > 0$  (C)  $b^2 - 4ac \geq 0$  (D)  $b^2 - 4ac < 0$
- (ix). If  $a_n = (-1)^n(n+1)$  then  $a_3 =$  \_\_\_\_\_.  
(A)  $3$  (B)  $-4$  (C)  $4$  (D)  $2$
- (x). True relation between Arithmetic Geometric and Harmonic Means is \_\_\_\_\_.  
(A)  $A > H > G$  (B)  $G > H > A$  (C)  $H > G > A$  (D)  $A > G > H$
- (xi).  $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots$  is the series of \_\_\_\_\_.  
(A) Arithmetic (B) Geometric (C) Harmonic (D) Neither of them
- (xii).  ${}^nC_r =$  \_\_\_\_\_.  
(A)  $\frac{1}{r!} \frac{n!}{r!}$  (B)  $\frac{n!}{r!}$  (C)  $\frac{n!}{r^{n-1}}$  (D)  $\frac{n!}{r^{r-1}}$
- (xiii). In the binomial expansion of  $(a+b)^n$  the number of terms are \_\_\_\_\_.  
(A)  $n+2$  (B)  $n+1$  (C)  $n$  (D)  $n-1$
- (xiv).  $\frac{-3\pi}{4}$  radians = \_\_\_\_\_.  
(a)  $130^\circ$  (b)  $-135^\circ$  (c)  $135^\circ$  (d)  $\frac{180}{\pi}$
- (xv).  $\cos(\alpha + \frac{\pi}{2}) =$  \_\_\_\_\_.  
(A)  $\cos \alpha$  (B)  $-\cos \alpha$  (C)  $\sin \alpha$  (D)  $-\sin \alpha$
- (xvi). Period of  $5 \sin 3x$  is \_\_\_\_\_.  
(A)  $2\pi$  (B)  $\frac{3\pi}{2}$  (C)  $-\pi$  (D)  $\frac{2\pi}{3}$
- (xvii). In law of tangents  $\frac{a+c}{a-c} =$  \_\_\_\_\_.  
(A)  $\tan(\frac{\alpha+\beta}{2})$  (B)  $\frac{\tan(\frac{\alpha+y}{2})}{\tan(\frac{\alpha-y}{2})}$  (C)  $\tan(\frac{\beta-y}{2})$  (D)  $\frac{\tan(\frac{\alpha-y}{2})}{\tan(\frac{\alpha+y}{2})}$
- (xviii). A circle drawn inside a triangle and touching the sides of a triangle is called \_\_\_\_\_.  
(A) In Circle (B) Circum Circle (C) Escribed Circle (D) None of these
- (xix). Domain of  $y = \sec x$  is \_\_\_\_\_.  
(a).  $[0, \pi]$  (b).  $[-\pi, \pi]$  (c).  $(-2\pi, 2\pi)$  (d).  $[0, \pi] - \frac{\pi}{2}$
- (xx).  $\cos^{-1}(-x) =$  \_\_\_\_\_.  
(a).  $\pi - \cos^{-1}x$  (b).  $\pi + \cos^{-1}x$  (c).  $\cos^{-1}x$  (d).  $-\cos^{-1}x$

**Mathematics Part-I**

Time: Allowed: 2.40h

Marks: 80

**SECTION "B"**

Marks: 50

**Q2. Answer any Ten (10) of the following Parts.**

- (i) if  $Z1 = a + ib$ ,  $Z2 = c + id$  then prove that  $\left[ \frac{\overline{Z1}}{Z2} \right] = \frac{\overline{Z1}}{Z2}$
- (ii)  $S = \{0, 1, 2, 3\}$  show that  $(S, +)$  is a Semi group. Where  $+$  defines addition Modulo 4.
- (iii) Find the inverse of the Matrix  $\begin{bmatrix} 4 & -2 & 5 \\ 2 & 1 & 0 \\ -2 & 2 & 3 \end{bmatrix}$  by using elementary row operation.
- (iv) Solve the equation  $(x-3)(x+9)(x+5)(x-7) = 385$
- (v) If  $\alpha, \beta$  are the roots of  $x^2 - 4x + 2 = 0$  then find the equation whose roots are  $\alpha + \frac{1}{\alpha}, \beta + \frac{1}{\beta}$
- (vi) Decompose  $\frac{x^2+3}{(x-1)(x^2+1)^2}$  into Partial fraction.
- (vii) Find four numbers in A.P such that their sum is 66 and the sum of their squares is 1214.
- (viii) Find the Sum to n terms of the series  $2.3.1 + 3.4.4 + 4.5.7 + \dots$
- (ix) Find the value of n when  ${}_4^np : {}_3^{n-1}p = 9:1$
- (x) Prove by Mathematical Indus that  $2^2 + 4^2 + 6^2 + \dots + (2n)^2 = \frac{2}{3}n(n+1)(2n+1)$
- (xi) Prove that  $\frac{\sin x - \cos x}{\tan^2 x - 1} = \frac{\cos^2 x}{\sin x - \cos x}$
- (xii) Show that  $\sin 5\theta + 2 \sin 3\theta + \sin \theta = 4 \sin 3\theta \cos^2 \theta$
- (xiii) Use the law of cosines to prove that  $1 + \cos \alpha = \frac{(b+c+a)(b+c-a)}{2bc}$

**SECTION "C"**

Marks: 30

**Note: Attempt any THREE questions. All questions carry equal marks.**

- Q3. (A) Find real and imaginary Parts of  $\left( \frac{1-i\sqrt{3}}{1+i\sqrt{3}} \right)^4$  (B) Solve the Matrix equation for x
- $$x \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix} - \begin{bmatrix} 3 & 2 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} -1 & 3 \\ 4 & 5 \end{bmatrix}$$

- Q4. (A) if  $n+1$ , and  $x-2$  are the factors of the polynomial  $x^3 - mx^2 + nx + 2$  then using synthetic division to find the values of m & n.

- (B) If  $\frac{1}{y-x}, \frac{1}{2y}$  and  $\frac{1}{y-z}$  from an A.P. prove that x, y and z form a G.P.

- Q.5 (A) Find the term independent of x in the expansion of  $\left( \sqrt{x} + \frac{1}{3x} \right)^{10}$
- (B) If  $y = \frac{1}{2^2} + \frac{1.3}{2!} \cdot \frac{1}{2^4} + \frac{1.3.5}{3!} \cdot \frac{1}{2^6} + \dots$  then  $y^2 + 2y - 1 = 0$

- Q.6 (A) Prove  $\sin^2 \frac{\theta}{2} = \frac{\sin \theta \cdot \tan \frac{\theta}{2}}{2}$

- (B) The angle of elevation of a building is  $48^\circ$  from A and  $61^\circ$  from B. if AB is 20 m. Find the height of the building.